

Name: Key**Lesson 6.3 – Arranging Equations**

Standard Form $ax + by = c$

Slope-Intercept Form $y = mx + b$

Example: Change the following linear equation into Slope-Intercept Form. Then find the slope and y-intercept:

$$8x + 2y = 4$$

$$\begin{array}{r} -8x \\ -8x \end{array}$$

$$\frac{2y}{2} = \frac{-8x + 4}{2}$$

$$y = -4x + 2$$

$$m(\text{slope}) = -4$$

$$b(\text{y-int}) = 2$$

$$3x - 4y + 2 = 0$$

$$\begin{array}{r} -3x \\ -3x \end{array}$$

$$\frac{-4y + 2}{-4} = \frac{-3x}{-4}$$

$$\frac{-4y}{-4} = \frac{-3x - 2}{-4}$$

$$y = \frac{3}{4}x + \frac{1}{2}$$

$$m(\text{slope}) = \frac{3}{4}$$

$$b(\text{y-int}) = \frac{1}{2} \text{ or } 0.5$$

Assignment:

Change the following linear equations into Slope-Intercept Form. Then find the slope and y-intercept:

$12x + 3y = 6$ $3y = -12x + 6$ $y = \frac{-12}{3}x + \frac{6}{3}$ $y = -4x + 2$ $\text{slope} = -4$ $\text{y-int} = 2$	$-5x - y + 3 = 0$ $-y + 3 = 5x$ $-y = 5x - 3$ $y = -5x + 3$ $\text{slope} = -5$ $\text{y-int} = 3$
$-3x + 9y = -6$ $9y = 3x - 6$ $y = \frac{3}{9}x - \frac{6}{9}$ $y = \frac{1}{3}x - \frac{2}{3}$ $\text{slope} = \frac{1}{3}$ $\text{y-int} = -\frac{2}{3}$	BONUS $0.9x - 0.3y = 1.2$ $\times 10 \quad \times 10 \quad \times 10$ $9x - 3y = 12$ $-3y = -9x + 12$ $y = 3x - 4$ $\text{slope} = 3$ $\text{y-int} = -4$

Arranging Equations

Standard Form $ax + by = c$

Slope-Intercept Form $y = mx + b$

Example: Change the following linear equation into Standard Form. Then find the x and y intercepts:

$y = 2x + 4$ $\begin{matrix} -2x & -2x \\ -2x + y = 4 \end{matrix}$ <p>Convention: make it positive</p> $2x - y = -4$ <p>Y-intercept</p> $2(0) - y = -4$ $y = 4$ <p>X-intercept</p> $2x - (0) = -4$ $x = -2$	$4y = -\frac{3}{4}x + 5$ $\begin{matrix} 4y = -3x + 20 \\ +3x & +3x \end{matrix}$ $3x + 4y = 20$ <p>Y-intercept</p> $3(0) + 4y = 20$ $y = 5$ <p>X-intercept</p> $\frac{3x}{3} + \frac{4(0)}{3} = \frac{20}{3}$ $x = \frac{20}{3}$
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Assignment:

Change the following linear equation into Standard Form. Then find the x and y intercepts:

$y = -3x + 1$ $3x + y = 1$ Yint $3(0) + y = 1$ $y = 1$ Xint $3x + (0) = 1$ $x = \frac{1}{3}$	$y = \frac{1}{2}x - 5$ $2y = x - 10$ $-x + 2y = -10$ $x - 2y = 10$ Yint $(0) - 2y = 10$ $y = -5$ Xint $x - 2(0) = 10$ $x = 10$
$y = -\frac{5}{3}x + 7$ $3y = -5x + 21$ $5x + 3y = 21$ Yint $y = 7$ Xint $x = \frac{21}{5}$	BONUS (no decimals in answer please) $y = 0.25x + 1.15$ $20y = 5x + 23$ $-5x + 20y = 23$ $5x - 20y = -23$ Yint $y = \frac{23}{20}$ Xint $x = -\frac{23}{5}$

Word Problems:

Translating an English sentence into a Linear Equation...

STEP #1: Define the variable

STEP #2: Start with what it equals

STEP #3: Write the equation

STEP #4: Draw the graph

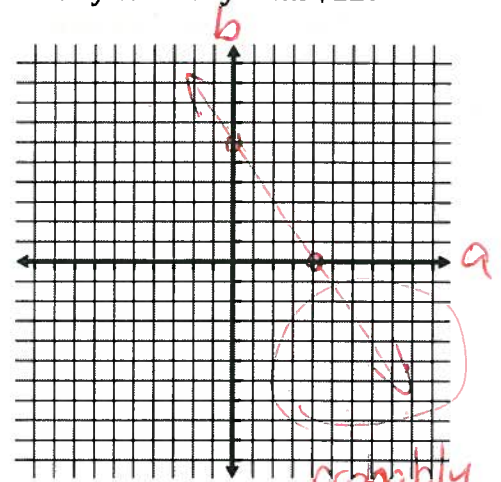
Example:

A bag of apples cost \$3 and a bunch of bananas cost \$2. How many can I buy with \$12?

a = apples, b = bananas

$$3a + 2b = 12$$

Bintercept $(b=6)$
 Aintercept $(a=4)$

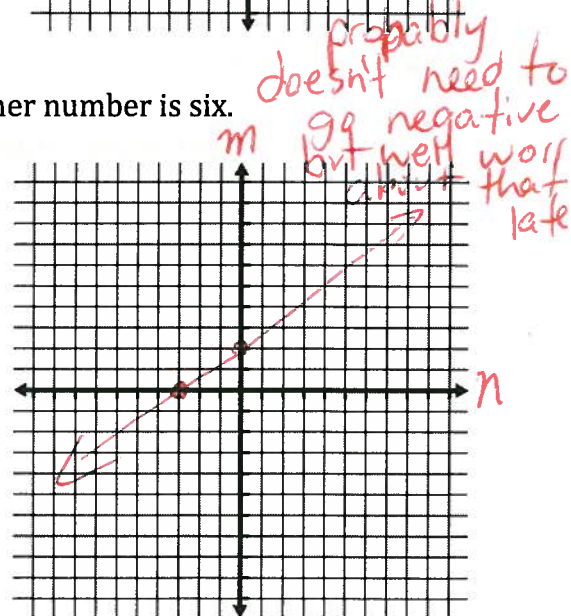


The difference between double a number and triple another number is six.

*n = one number
 m = another number*

$$3m - 2n = 6$$

Mintercept = 2
 Nintercept = -3



Assignment:

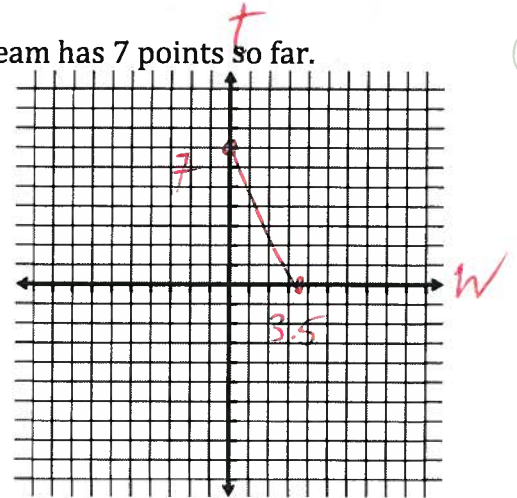
Wins are worth 2 points and ties are worth 1 point. My team has 7 points so far.

$w = \text{wins}$ $t = \text{ties}$

$$2w + t = 7$$

Tintercept = 7

Wintercept = 3.5



The difference between half of one number and triple another number is three.

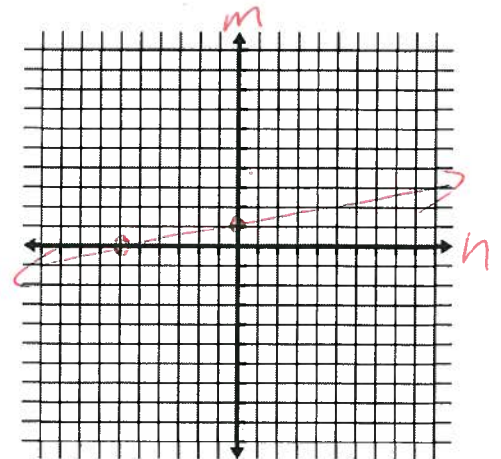
$n = \text{one number}$

$m = \text{another number}$

$$3m - \frac{1}{2}n = 3$$

Mintercept = 1

Nintercept = -6



You have pennies and nickels worth a total of ten cents.

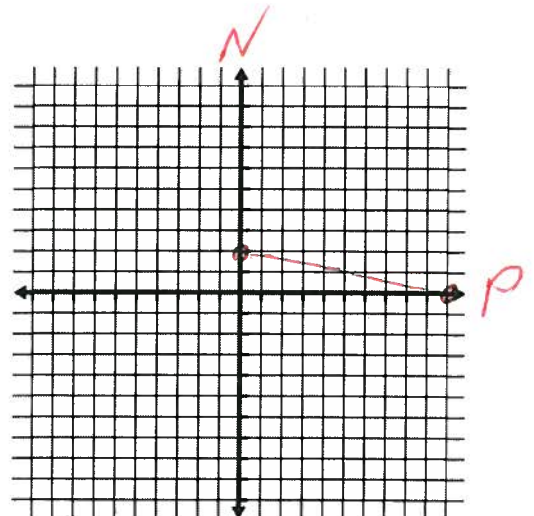
$p = \text{pennies}$

$n = \text{nickels}$

$$p + 5n = 10$$

Pintercept = 10

nintercept = 2



Practice Quiz:

Change the following linear equation into Standard Form. Then find the x and y intercepts:

$$y = -\frac{2}{3}x + 4$$

$$3y = -2x + 12$$

$$2x + 3y = 12$$

Xintercept $2x + 3(0) = 12$

$$x = 6$$

Yintercept $2(0) + 3y = 12$

$$y = 4$$

Change the following linear equation into Slope Intercept Form. Then find the slope and the y-intercept:

$$2x - 3y = 9$$

$$-3y = -2x + 9$$

$$y = -\frac{2}{3}x + \frac{9}{3}$$

$$y = \frac{2}{3}x - 3$$

slope = $\frac{2}{3}$

y intercept = -3

Write a linear equation and draw the corresponding graph:

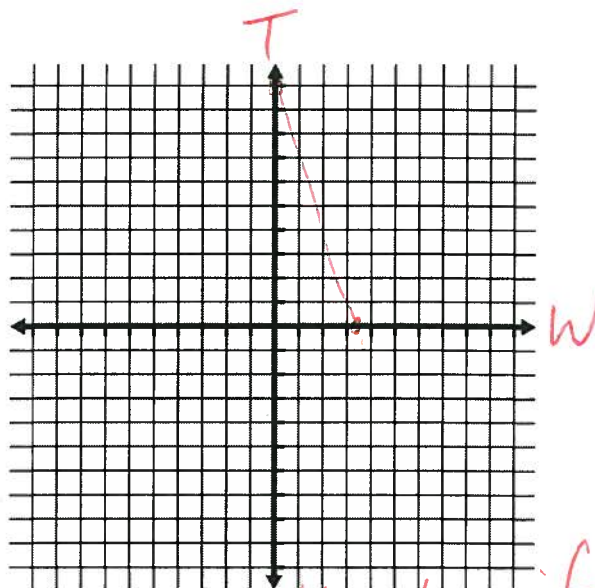
Wins are worth 3 points and ties are worth 1 point. My team has 10 points so far.

w = wins
t = ties

$$3w + t = 10$$

Tintercept = 10

Wintercept = $\frac{10}{3} = 3.3$



It's okay if you put arrows on graph paper. We'll sort that out later.

