## Chapter 7: Quadratics

Name: $\qquad$

## Notes 7.2 Analyzing a Graph

Quadratic $=$
NOT
Parabola $=$
Regular Pattern:
Vertex $=$
Minimum or Maximum
Axis of Symmetry =
Equation for the Axis of Symmetry:
Domain $=$
All quadratic equations have a domain of $\qquad$
Range $=$
All quadratic equations have a range limited by $\qquad$
Intercepts $=$
$Y$-Intercept $=\quad X$-Intercept $=$
Vertex Form =
The vertex form is used for $\qquad$
Standard Form $=$
The standard form is $\qquad$

Using your calculator:
Example \#1: Create a table of values and graph the parabola

$$
y=-\frac{1}{2}(x+1)^{2}+2
$$

| $x$ | $y$ |
| :---: | :---: |
|  |  |
|  |  |
|  |  |



Example \#2: Analyze the graph and write an equation to match:


Vertex:
Axis of Symmetry:
Y-Intercept:
X-Intercepts:
Domain:

Range:
Pattern:
Equation:

Example \#3: Analyze the equation $y+4=2(x-2)^{2}$
a) Arrange the equation so that it follows the vertex form of $y=a(x-p)^{2}+q$
b) Sketch the graph and indicate your window size:

c) Use your calculator to determine the vertex:
d) What is the equation for the Axis of Symmetry?
e) What are the $x$ and $y$ intercepts for the graph?
e) What is the domain and range of the graph?
f) What is the pattern that each value goes up by?

## Assignment

## Part 1:

1) Which graphs appear to represent quadratic relations? (parabolas)
a)

c)

e)

b)

d)

f)

2) Which of the following relations are quadratic?
a) $y=2 x-7$
b) $y=2 x(x+3)$
c) $y=(x+4)^{2}+1$
d) $y=x^{2}-5 x-x$
e) $y=4 x^{3}+x^{2}-x$
f) $y=x(x+1)^{2}-7$
3) Find the $y$-intercept for each quadratic relation in \#2 (HINT: when $x=0$ )
a)
b)
c)
d)
e)
f)
4) Explain why $a$ cannot be zero for a quadratic in the form of

$$
y=a x^{2}+b x+c
$$

5) Does the parabola open up or down?
a) $y=x^{2}-4$
b) $y=-2 x^{2}+6 x$
c) $y=9-x+3 x^{2}$
d) $y=-\frac{2}{3} x^{2}-6 x+1$
6) Does each parabola open up or down?
a)

| $\boldsymbol{x}$ | -4 | -3 | -2 | -1 | 0 | 1 |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $\boldsymbol{y}$ | 12 | 5 | 0 | -3 | -4 | -3 |

b)

| $\boldsymbol{x}$ | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $\boldsymbol{y}$ | -13 | -3 | 3 | 5 | 3 | -3 |

c)

| $\boldsymbol{x}$ | -5 | -4 | -3 | -2 | -1 | 0 |
| :---: | :---: | :--- | :--- | :--- | :--- | :---: |
| $\boldsymbol{y}$ | 3.0 | -0.5 | -3.0 | -4.5 | -5.0 | -4.5 |

d)

| $\boldsymbol{x}$ | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{y}$ | -4 | 19 | 40 | 59 | 76 | 91 |

## Part 2:

1) Analyze the following parabola:

a) equation of the axis of symmetry $=$ $\qquad$
b) Vertex:
c) Domain: $\qquad$ Range: $\qquad$
2) State the coordinates of the $y$-intercept and two additional points for each function
a) $f(x)=2 x^{2}+8 x+8$

$$
y \text {-intercept }=
$$

| $x$ | $y$ |
| :---: | :---: |
|  |  |

b) $f(x)=4 x-x^{2}$

$$
\mathrm{y} \text {-intercept }=\overline{\text { two other points }}
$$

| $x$ | $y$ |
| :---: | :---: |
|  |  |
|  |  |

3) Analyze each of the following


| x-intercept |  |
| :--- | :--- |
| $y$-intercept |  |
| Axis of Symmetry |  |
| Vertex |  |
| Domain |  |
| Range |  |

4) Analyze each of the following:

## a) <br> 

| Axis of Symmetry |  |
| :--- | :--- |
| Vertex |  |
| Domain |  |
| Range |  |



| x-intercept |  |
| :--- | :--- |
| $y$-intercept |  |
| Axis of Symmetry |  |
| Vertex |  |
| Domain |  |
| Range |  |

b)


| Axis of Symmetry |  |
| :--- | :--- |
| Vertex |  |
| Domain |  |
| Range |  |

## c)


d)


| Axis of Symmetry |  |
| :--- | :--- |
| Vertex |  |
| Domain |  |
| Range |  |

6) Find the minimum or maximum value
a)

b)

$c$


## Answers:

## Part 1

1. a) not a quadratic relation
d) quadratic relation
b) not a quadratic relation
e) quadratic relarion
c) not a quadratic relation
f) not a quadratic relation
2. a) not a quadratic relation
d) quadratic relation
b) quadratic relation
e) not a quadratic relation
c) quadratic relation
f) not a quadratic relation
3. b) 0
c) 17
d) -6
4. e.g., If $a=0$, then $y=b x+c$, which is a linear rela: on, not a quadratic relation.
5. a) up, $a>0$
c) up, $a>0$
b) down, $a<0$
d) down, $a<0$
6. a) up
c) up
b) down
d) down

Part 2

1. a) $x=4$
b) $(4,-16)$
2. a) $(0,8)$; e.g., $(1,18),(-1,2)$
b) $(0,0)$; e.g., $(1,3),(-1,-5)$
3. a) $(0,0),(2,0) ;(0,0) ; x=1 ;(1,-2) ;\{(x, y) \mid x \in \mathrm{R}, y \geq-2, y \in \mathrm{R}\}$
b) $(-1,0),(6,0) ;(0,4.5) ; x=2.5 ;(2.5,9.2)$;
$\{(x, y) \mid x \in \mathrm{R}, y \leq 9.2, y \in \mathrm{R}\}$
4. a) $x=2 ;(2,-1) ;\{(x, y) \mid x \in \mathrm{R}, y \geq-1, y \in \mathrm{R}\}$
b) $x=4$; $(4,28) ;\{(x, y) \mid x \in R, y \leq 28, y \in R\}$
c) $x=3$; $(3,-1) ;\{(x, y) \mid x \in \mathrm{R}, y \leq-1, y \in \mathrm{R}\}$
d) $x=2.5 ;(2.5,-12.25) ;\{(x, y) \mid x \in R, y \geq-12.25, y \in R\}$
5. a) graph $\mathrm{d}_{;}(2.5,-12.25)$
c) $\operatorname{graph} \mathrm{c}$; $(3,-1)$
b) graph $b_{i}(4,28)$
d) graph a; $(2,-1)$
6. a) maximum of 4
b) minimum of -3
c) maximum of 2

## Practice Quiz

Analyze the following quadratic equation and then draw the graph:
$y=-2(x+4)^{2}+8$

| Horizontal shift $(\boldsymbol{p})$ |  |
| :--- | :--- |
| Vertical shift (q) |  |
| Vertex |  |
| Stretch factor (a) |  |
| Compressed Vertically <br> OR Stretched Vertically |  |
| Minimum (opens up) OR <br> Maximum (opens down) |  |
| Equation of the <br> Axis of Symmetry |  |
| Domain |  |
| Range |  |


| $x$ | $y$ |
| :--- | :--- |
|  |  |
|  |  |
|  |  |



